

## Chapter 10 Solutions

### Section 10.1

1.  $H_0$ : The proportion of students signing up for Math 72 is the same for each semester.

$H_j$ : At least one proportion is different from the others.

The sample size is  $n = \sum O = 530$ . Dividing this into equal proportions amongst classes gives an expected frequency of  $E = 530/7 = 75.714$

$O = \text{Observed Frequencies}$	$E = \text{Expected Frequencies}$	$(O-E)^2/E$
41	75.714	15.91617251
75	75.714	0.006738544
159	75.714	91.61428571
67	75.714	1.00296496
112	75.714	17.38975741
37	75.714	19.79541779
39	75.714	17.80296496
	$\chi^2 = \sum(O-E)^2/E =$	163.528301

The test statistic is  $\chi^2 = \sum(O-E)^2/E = 163.5283$

There are  $k = 7$  categories resulting  $d.f. = 6$ .  $\alpha = 0.05$

The critical value is  $\chi^2 = 12.5916$ ; The  $p$ -value is  $1.05925 \cdot 10^{-32}$

We reject the null hypothesis. *The data do not support the claim that the proportions of students signing up for Math 72 were the same for each semester offered.*

3.  $H_0$ : The sample is drawn from a normal population, so proportions in the specified intervals match the empirical rule.

$H_j$ : The sample is not drawn from a normal population, so proportions in the specified intervals differ significantly from the empirical rule.

$O = \text{Observed Frequencies}$	$E = \text{Expected Frequencies}$	$(O-E)^2/E$	Alpha	Number of Categories
1	1.3	0.069230769	0.05	6
1	7.02	5.162450142		
29	17.68	7.247873303		
17	17.68	0.026153846		
2	7.02	3.58980057		
2	1.3	0.376923077		
Test Statistic:	$\chi^2 = \sum(O-E)^2/E =$	16.47243171		
			Critical Value $\chi^2 = 16.7496$	
			p-value 0.005617049	

The test statistic is  $\chi^2 = \sum(O-E)^2/E = 16.4724$

There are  $k = 6$  categories resulting  $d.f. = 5$ .  $\alpha = 0.005$

The critical value is  $\chi^2 = 16.7496$ ; The  $p$ -value is 0.00562

We fail to reject the null hypothesis. *At the chosen level of significance, we are unable to reject the claim that the sample is taken from a normal population. Still, the  $p$ -value was quite small, indicating some significant departures from the frequencies expected from a perfectly normal sample.*

5.  $H_0$ : The coin is unbiased, so proportions of numbers of heads out of five should be those predicted by the binomial distribution with  $n = 5$ , and  $p = 0.5$ .  
 $H_j$ : The coin is biased, so the proportions do not match those predicted by the binomial distribution.

O=Observed Frequencies	E=Expected Frequencies	(O-E) <sup>2</sup> /E	Alpha	Number of Categories
59	62.5	0.196	0.05	6
316	312.5	0.0392		
596	625	1.3456		
663	625	2.3104		
320	312.5	0.18		
76	62.5	2.916		
Test Statistic: $\chi^2 = \sum(O-E)^2/E =$				
		6.9872		

  

Critical Value 11.07049775
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p-value 0.221594008
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The test statistic is  $\chi^2 = \sum(O-E)^2/E = 6.9872$

There are  $k = 6$  categories resulting  $d.f. = 5$ .  $\alpha = 0.05$

The critical value is  $\chi^2 = 11.0705$ ; The  $p$ -value is 0.2215

We fail to reject the null hypothesis. *We are unable to reject the claim that the coin is unbiased, so proportions of numbers of heads out of five are those predicted by the binomial distribution with  $n = 5$ , and  $p = 0.5$ .*

## Section 10.2

1.  $H_0$ : Marijuana use is independent of political views.  
 $H_1$ : They are dependent

**Observed Frequencies**

	Never	Rarely	Frequently	Totals
Liberal	479	173	119	771
Conservative	214	47	15	276
Other	172	45	85	302
Totals	865	265	219	1349

**Expected Frequencies**

	Never	Rarely	Frequently
Liberal	494.3773	151.4566	125.166
Conservative	176.9755	54.21794	44.80652
F=Other	193.6471	59.32543	49.02743

**$(O-E)^2/E$**

	Never	Rarely	Frequently
Liberal	0.478302	3.064353	0.303758
Conservative	7.745764	0.960912	19.82811
Other	2.41986	3.459189	26.39392

<b>D.F.:</b> 4	<b>Chi-Square T.S.:</b> 64.6542	<b>p-value</b>
<b>Alpha:</b> 0.01	<b>Chi-Square C.V.:</b> 13.2767	3.04E-13

The test statistic is  $\chi^2 = \sum(O-E)^2/E = 64.6542$

There are 3 rows and 3 columns resulting in  $d.f. = (3 - 1)(3 - 1) = 4$ .  $\alpha = 0.01$

The critical value is  $\chi^2 = 13.2767$ ; The  $p$ -value is  $3.04 \cdot 10^{-13} = 0.000000000000304$ .

Reject the null hypothesis. The data do not support the claim that marijuana use is independent of political views. The dependency is highly significance and indicated by the extraordinarily small  $p$ -value.

3.  $H_0$ : Grades are independent of gender.

$H_1$ : They are dependent

Observed Frequencies			
	female	male	Totals
A	3	3	6
B	19	18	37
C	19	21	40
D	4	10	14
Totals	45	52	97

Expected Frequencies		
	female	male
A	2.783505	3.216495
B	17.16495	19.83505
C	18.5567	21.4433
D	6.494845	7.505155

$(O-E)^2/E$		
	female	male
A	0.016838	0.014572
B	0.19618	0.169771
C	0.01059	0.009164
D	0.958337	0.82933

<b>D.F.:</b>	3	<b>Chi-Square T.S.:</b>	2.2048	<b>p-value</b>
<b>Alpha:</b>	0.01	<b>Chi-Square C.V.:</b>	11.3449	0.5310

The test statistic is  $\chi^2 = \sum(O-E)^2/E = 2.2048$

There are 4 rows and 2 columns resulting in  $d.f. = (4 - 1)(2 - 1) = 3$ .  $\alpha = 0.01$

The critical value is  $\chi^2 = 11.3449$ ; The  $p$ -value is  $3.04 \cdot 10^{-13} = 0.5310$ .

Fail to reject the null hypothesis. The data make it evident that grades are not dependent on gender.

5.  $H_0$ : Survival is independent of gender.

$H_1$ : They are dependent

**Observed Frequencies**

	Survived	Died	Totals
Male	23	29	52
Female	25	9	34
Totals	48	38	86

**Expected Frequencies**

	Survived	Died
Male	29.02326	22.97674
Female	18.97674	15.02326

**$(O-E)^2/E$**

	Survived	Died
Male	1.250019	1.578971
Female	1.911793	2.414897

<b>D.F.:</b>	1	<b>Chi-Square T.S.:</b>	7.1557	<b>p-value</b>
<b>Alpha:</b>	0.01	<b>Chi-Square C.V.:</b>	6.6349	0.00747

The test statistic is  $\chi^2 = \sum(O-E)^2/E = 7.1557$

There are 2 rows and 2 columns resulting in  $d.f. = (2 - 1)(2 - 1) = 1$ .  $\alpha = 0.01$

The critical value is  $\chi^2 = 6.6349$ ; The  $p$ -value is 0.00747.

Reject the null hypothesis. It appears that survival is dependent on gender.